Irregular labeling of digraphs

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Let \overrightarrow{G} be a directed graph of order n with no component of order less than 4, and let Γ be a finite Abelian group such that $|\Gamma| \ge n + 6$. We show that there exists a mapping ψ from the arc set $E(\overrightarrow{G})$ of \overrightarrow{G} to an Abelian group Γ such that if we define a mapping φ_{ψ} from the vertex set $V(\overrightarrow{G})$ of \overrightarrow{G} to Γ by

$$\varphi_{\psi}(x) = \sum_{y \in N^{+}(x)} \psi(xy) - \sum_{y \in N^{-}(x)} \psi(yx), \quad (x \in V(\overrightarrow{G})),$$

then φ_{ψ} is injective.